

Differentiation formula

$$\frac{d}{dx}[C] = 0$$

$$\frac{d}{dx}[kx] = k$$

$$\frac{d}{dx}[kf(x)] = kf'(x) \text{ a constant can be "factored out"}$$

$$\frac{d}{dx}[f(x) \pm g(x)] = f'(x) \pm g'(x)$$

the derivative of a sum is the sum of derivatives

$$\frac{d}{dx}[x^n] = nx^{n-1} \text{ - the power rule}$$

Integration formula

$$\int 0 \, dx = C$$

$$\int k \, dx = kx + C$$

$$\int kf(x) \, dx = k \int f(x) \, dx + C \text{ - factor out constant}$$

$$\int [f(x) \pm g(x)] \, dx = \int f(x) \, dx + \int g(x) \, dx + C$$

integral of a sum is the sum of the integrals

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C \text{ - the power rule reversed}$$

Differentiation formula

$$\frac{d}{dx}[\sin x] = \cos x$$

$$\frac{d}{dx}[\cos x] = -\sin x$$

$$\frac{d}{dx}[\tan x] = \sec^2 x$$

$$\frac{d}{dx}[\csc x] = -\csc x \cot x$$

$$\frac{d}{dx}[\sec x] = \sec x \tan x$$

$$\frac{d}{dx}[\cot x] = -\csc^2 x$$

Integration formula

$$\int \cos x \, dx = \sin x + C$$

$$\int \sin x \, dx = -\cos x + C$$

$$\int \sec^2 x \, dx = \tan x + C$$

$$\int \csc x \cot x \, dx = -\csc x + C$$

$$\int \sec x \tan x \, dx = \sec x + C$$

$$\int \csc^2 x \, dx = -\cot x + C$$

So we have a new differentiation rule - the ln rule:

$$\frac{d}{dx}[\ln x] = \frac{1}{x}, x > 0$$

$$\frac{d}{dx}[\ln u] = \frac{1}{u} \cdot \frac{du}{dx} = \frac{u'}{u}, u > 0$$

$$\frac{d}{dx}[\ln|u|] = \frac{1}{u} \cdot \frac{du}{dx} = \frac{u'}{u}, u \neq 0$$

$$\int \frac{1}{x} \, dx = \ln|x| + C \text{ and if } u \text{ is a differentiable function of } x, \int \frac{1}{u} \, du = \ln|u| + C$$

$$\frac{d}{dx}[e^x] = e^x \text{ and if } u \text{ is a differentiable function of } x \text{ then } \frac{d}{dx}[e^u] = e^u \frac{du}{dx}$$

$$\int e^x dx = e^x + C \text{ and if } u \text{ is a differentiable function of } x \text{ then } \int e^u du = e^u + C$$

$$\frac{d}{dx} a^x = a^x \cdot \ln a \quad \text{and} \quad \frac{d}{dx} a^u = a^u \cdot \ln a \cdot \frac{du}{dx}$$

The derivatives of the three inverse trig functions are as follows:

$$\begin{aligned} \frac{d}{dx}(\sin^{-1} u) &= \frac{1}{\sqrt{1-u^2}} \frac{du}{dx} \\ \frac{d}{dx}(\cos^{-1} u) &= \frac{-1}{\sqrt{1-u^2}} \frac{du}{dx} \\ \frac{d}{dx}(\tan^{-1} u) &= \frac{1}{1+u^2} \frac{du}{dx} \end{aligned}$$

If u is a differentiable function of x , and $a > 0$ then

$$\begin{aligned} \int \frac{du}{\sqrt{a^2 - u^2}} &= \sin^{-1} \frac{u}{a} + C \\ \int \frac{du}{a^2 + u^2} &= \frac{1}{a} \tan^{-1} \frac{u}{a} + C \end{aligned}$$